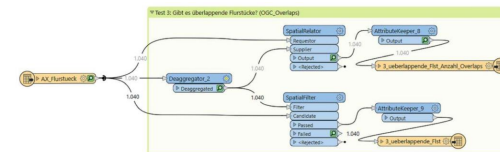
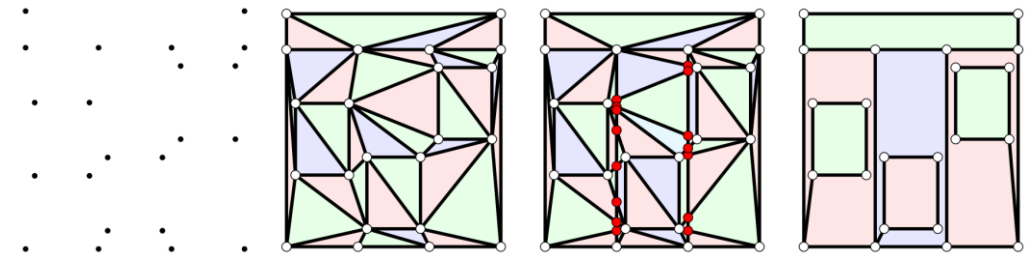
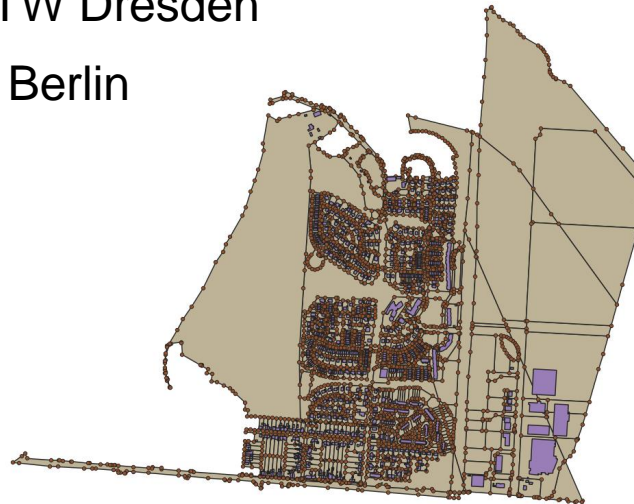


A computational robust method for spatial decomposition - Test case with cadastral data

Enrico Romanschek, HTW Dresden

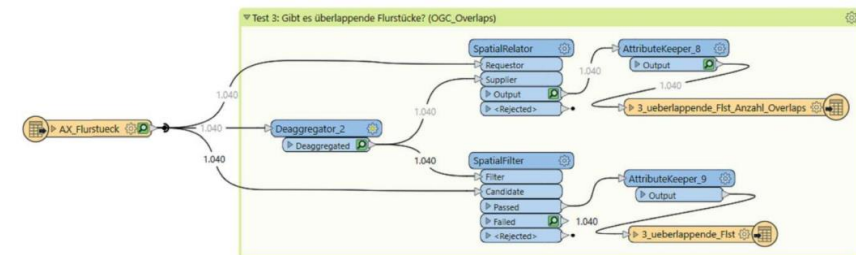
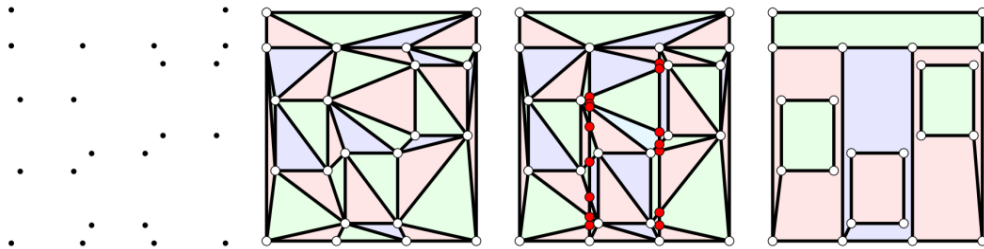
Christian Clemen, HTW Dresden

Wolfgang Huhnt, TU Berlin



Agenda

- // 1. Standard (GIS) vs. space decomposition.
- // 2. Short explanation how our algorithm works.
- // 3. Test cases with results and cross-check.
- // 4. Conclusion and Outlook.





Comparison

// Standard

- // Simple features (B-Rep) possibly with attached semantic data.

// Our Algorithm



Comparison

// Standard

- // Simple features (B-Rep) possibly with attached semantic data.
- // Simple features without topology.
- // Only features modeled.
- // Coordinates as floating-point numbers.
- // Intersections as computed coordinates with possible loss of precision.

// Our Algorithm



Comparison

// Standard

- // Simple features (B-Rep) possibly with attached semantic data.
- // Simple features without topology.
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// Our Algorithm

- // Complete, gapless and overlap-free two-dimensional space decomposition.



Comparison

// Standard

- // Simple features (B-Rep) possibly with attached semantic data.
- // Simple features without topology.
- // Only features modeled.
- // Coordinates as floating-point numbers.
- // Intersections as computed coordinates with possible loss of precision.

// Our Algorithm

- // Complete, gapless and overlap-free two-dimensional space decomposition.
- // A data structure that maps the topology.
- // Modeling even empty spaces as objects.
- // Exclusive use of integer coordinates.
- // Intersections as positions on edges and not by coordinates.
- // A special algorithm for reconstructing.



Comparison

// Standard

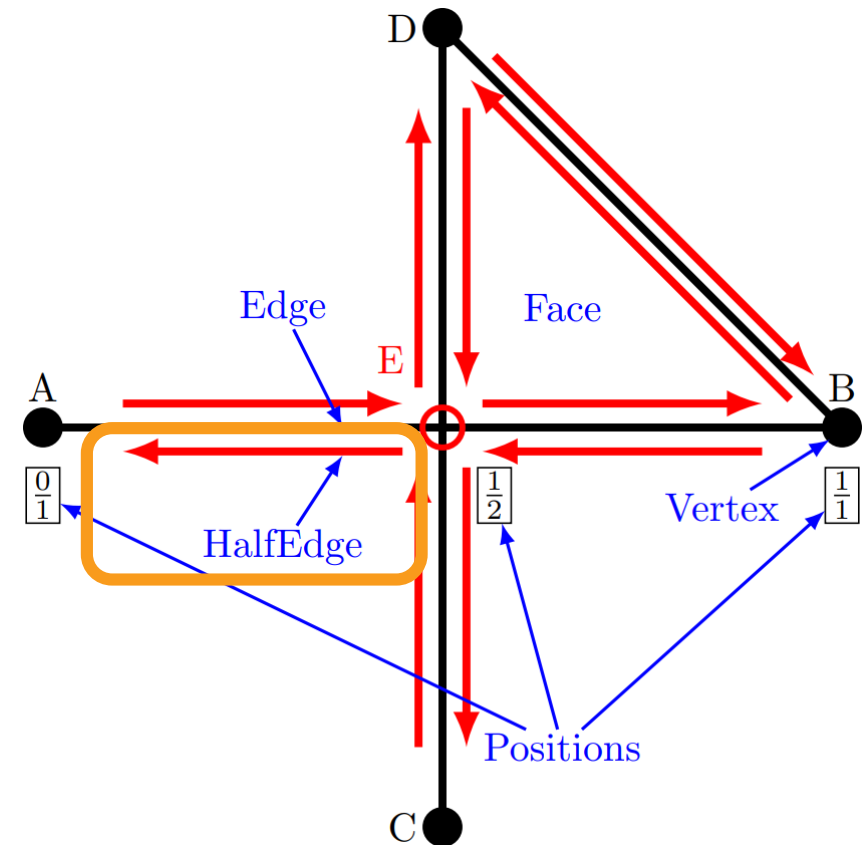
- // Simple features (B-Rep) possibly with attached semantic data.
- // Simple features without topology.
- // Only features modeled.
- // Coordinates as floating-point numbers.
- // Intersections as computed coordinates with possible loss of precision.
- // Spatial relations with error-prone numerical calculations.

// Our Algorithm

- // Complete, gapless and overlap-free two-dimensional space decomposition.
- // A data structure that maps the topology.
- // Modeling even empty spaces as objects.
- // Exclusive use of integer coordinates.
- // Intersections as positions on edges and not by coordinates.
- // A special algorithm for reconstructing.
- // Spatial relations with DE-9IM matrices as set operations.

Procedure – data structure

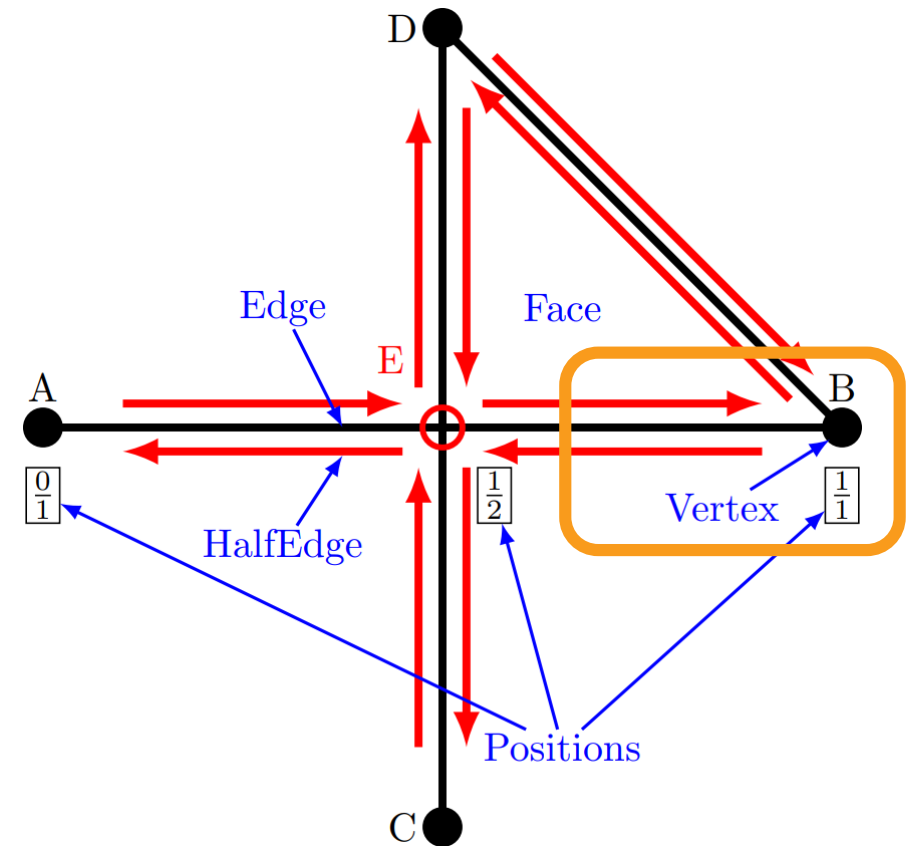
// Half-edges



Procedure – data structure

// Half-edges

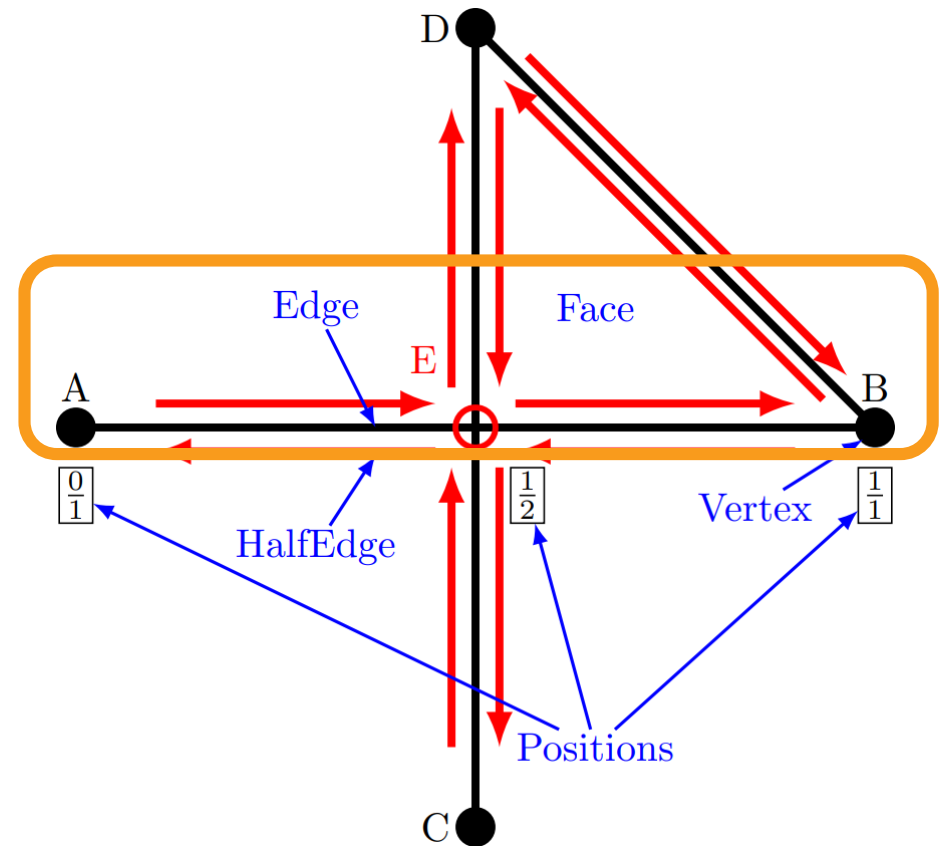
// Vertex



Procedure – data structure

// Half-edges

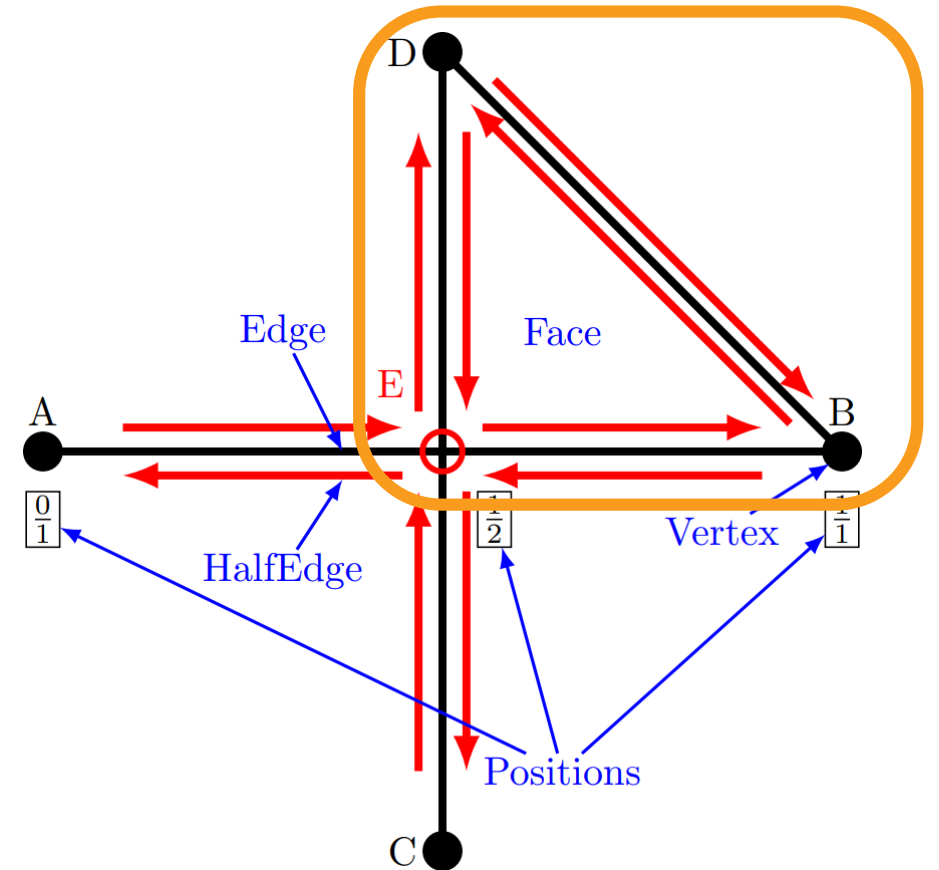
// Vertex, Edge



Procedure – data structure

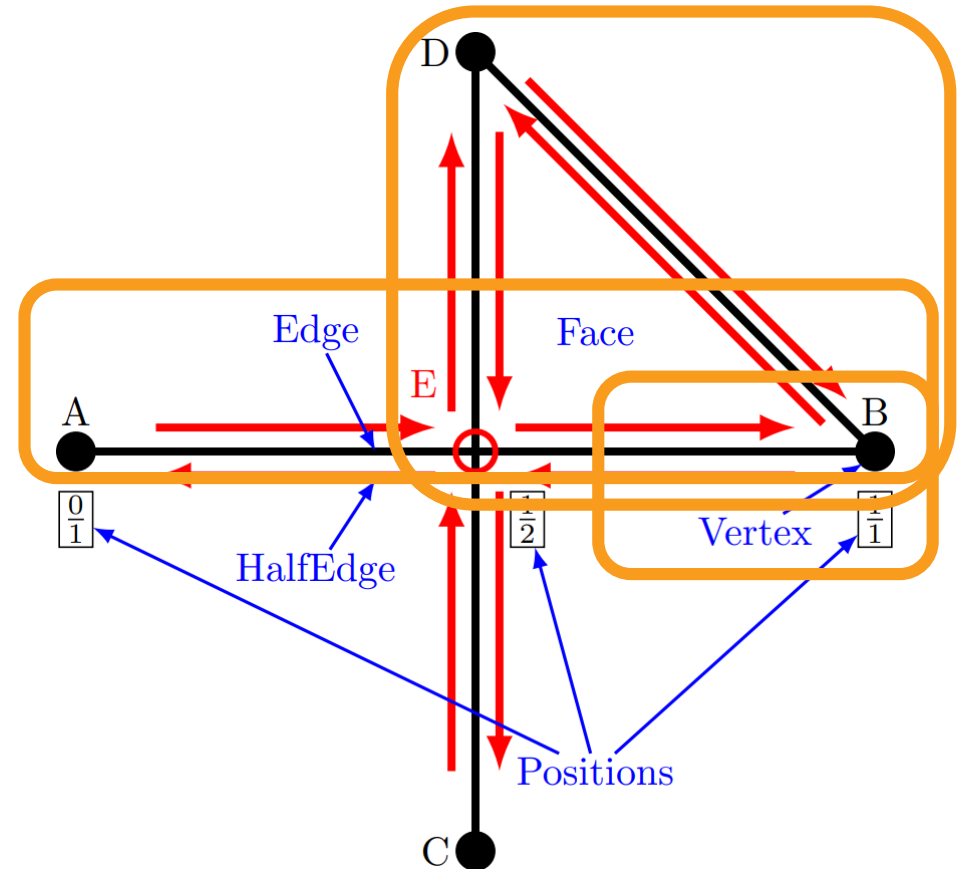
// Half-edges

// Vertex, Edge, Face



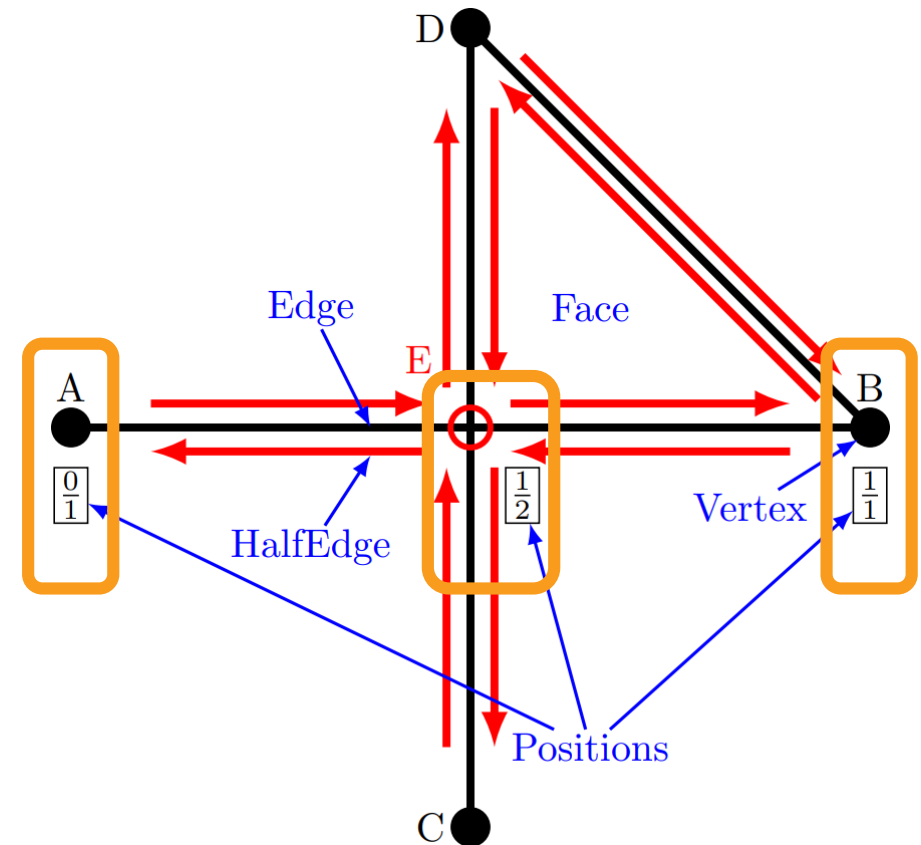
Procedure – data structure

- // Half-edges
- // Vertex, Edge, Face
- // with Ids of the origin data



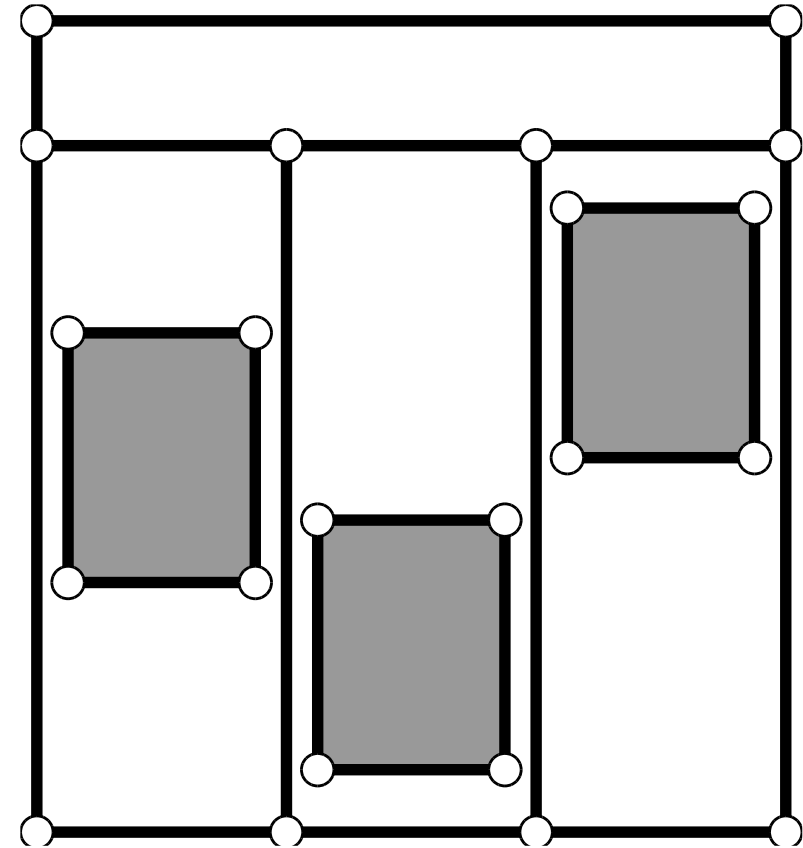
Procedure – data structure

- // Half-edges
- // Vertex, Edge, Face
- // with Ids of the origin data
- // Vertices as positions on edges



Procedure – initial data

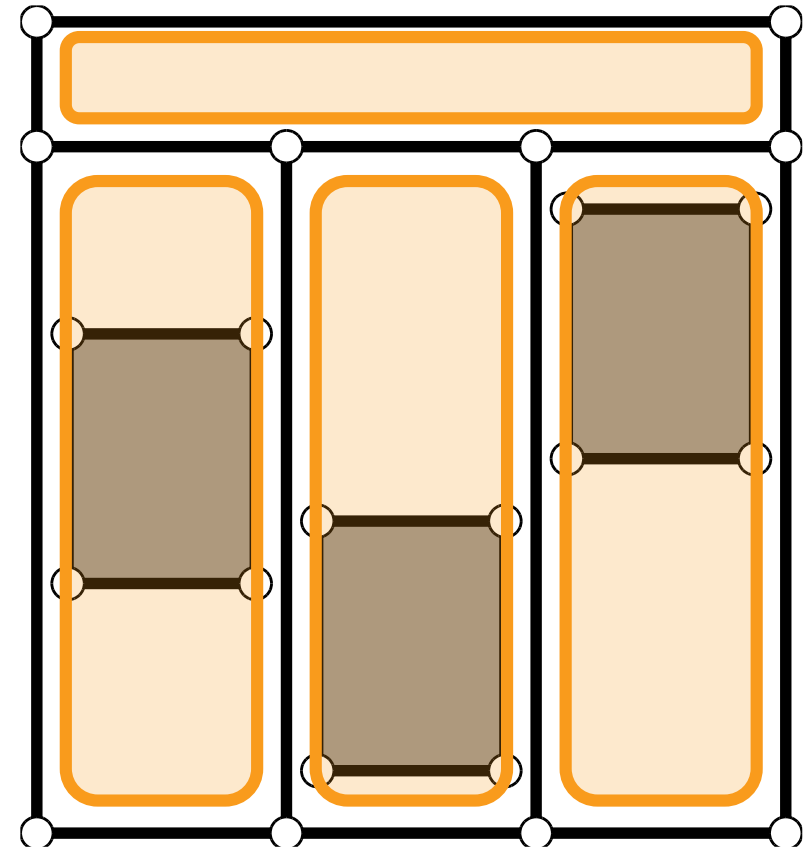
// 7 Polygons



Procedure – initial data

// 7 Polygons

// 4 Parcels

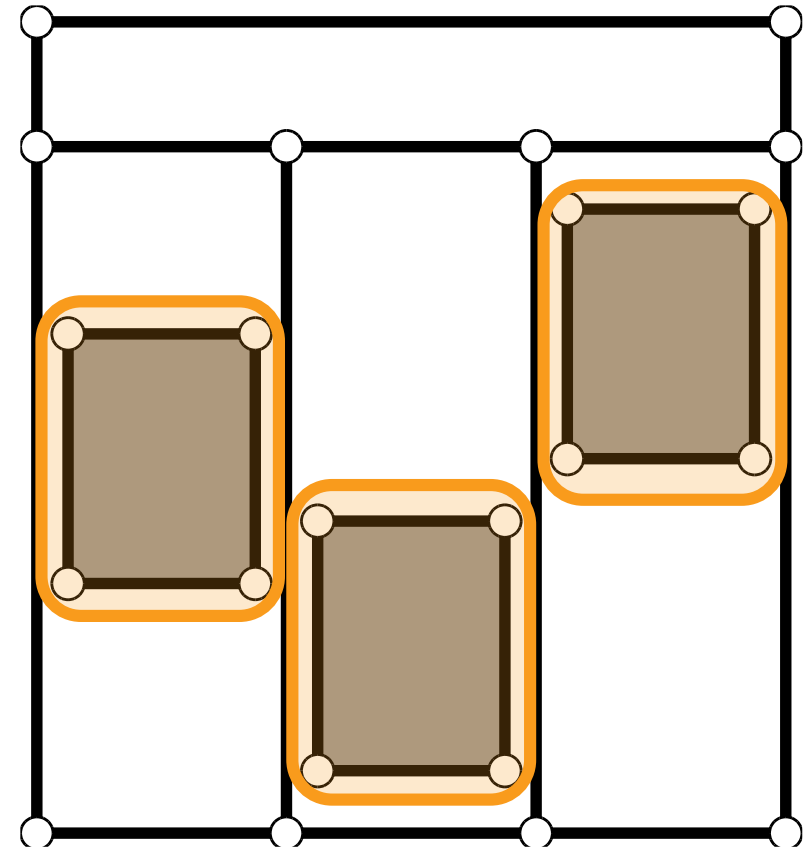


Procedure – initial data

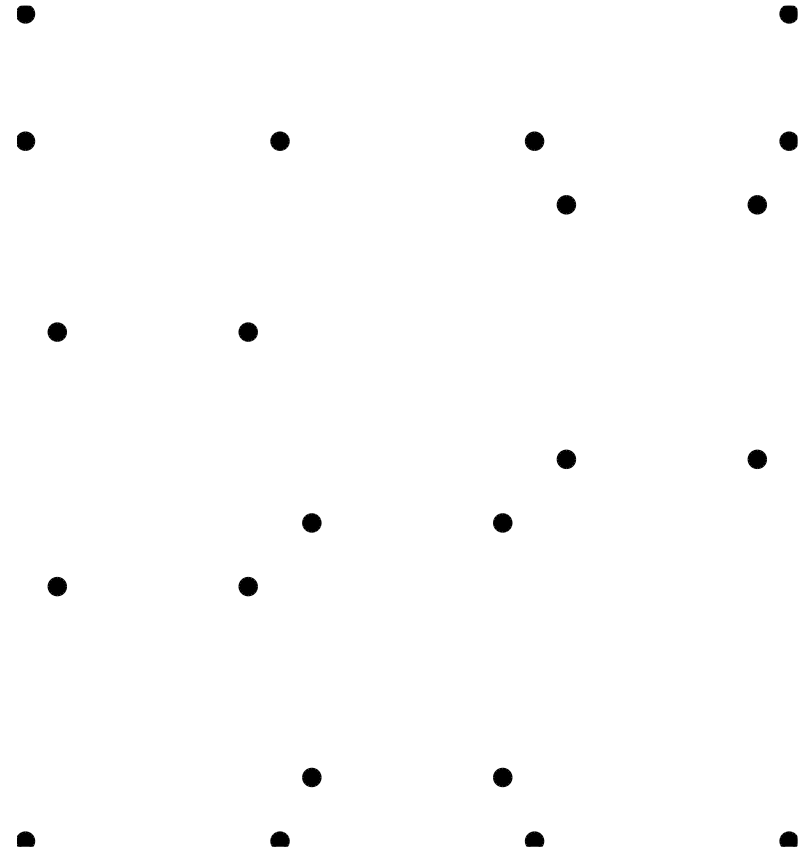
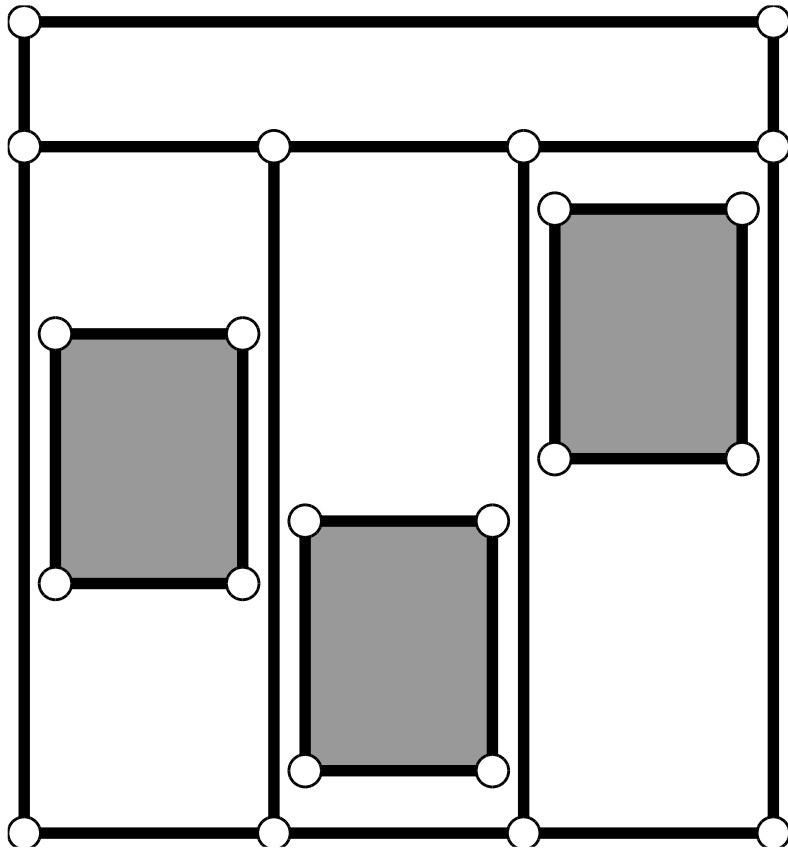
// 7 Polygons

// 4 Parcels

// 3 Buildings



Procedure – step 1 – integer coordinates

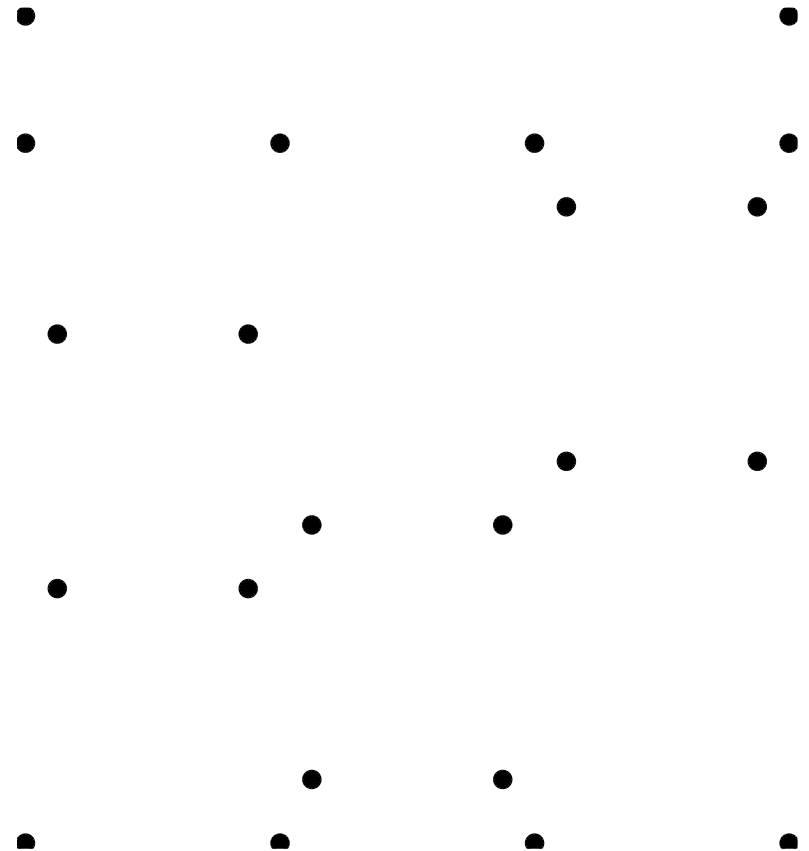


Procedure – step 1 – integer coordinates

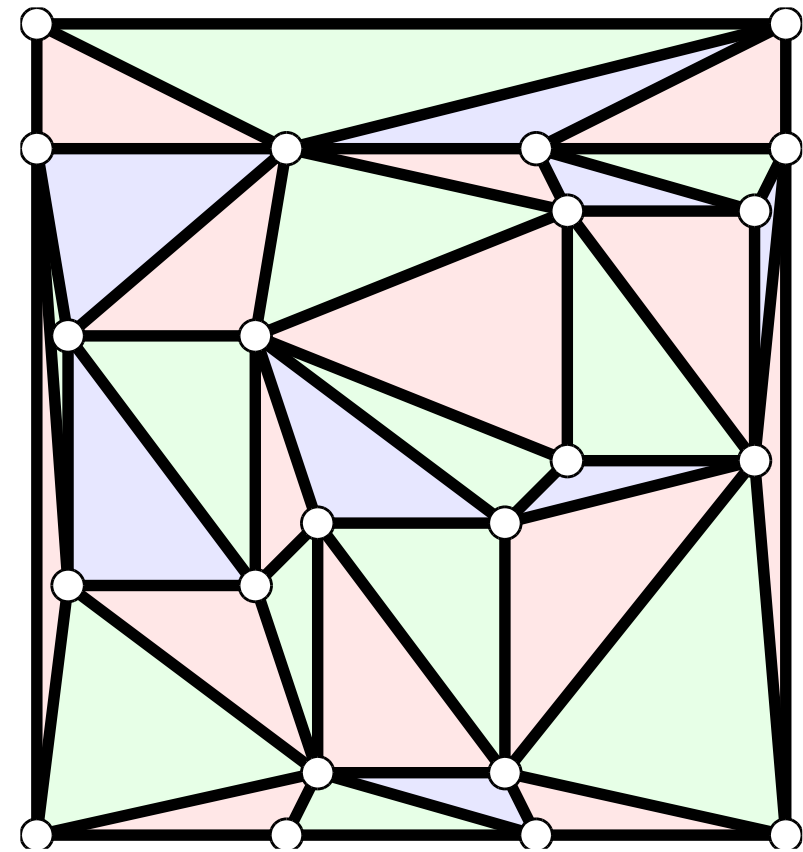
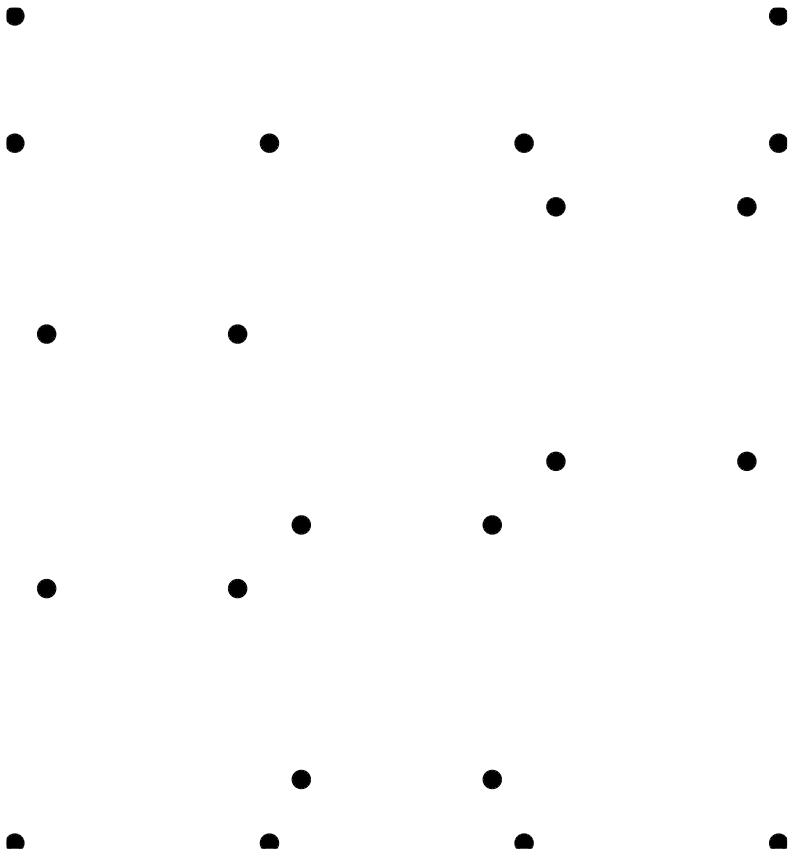
// 22 points

// Conversion from
floating point to integer

$$\begin{pmatrix} x_{int} \\ y_{int} \end{pmatrix} = scale \left[\begin{pmatrix} x_{float} \\ y_{float} \end{pmatrix} - \begin{pmatrix} x_{min} \\ y_{min} \end{pmatrix} \right]$$

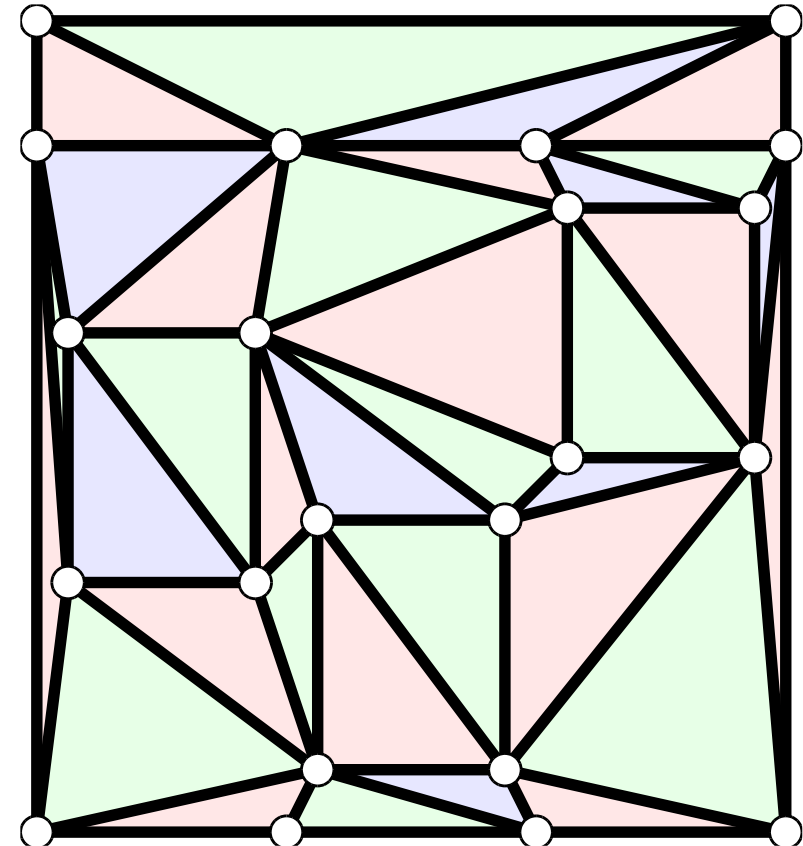


Procedure – step 2 – triangulation



Procedure – step 2 – triangulation

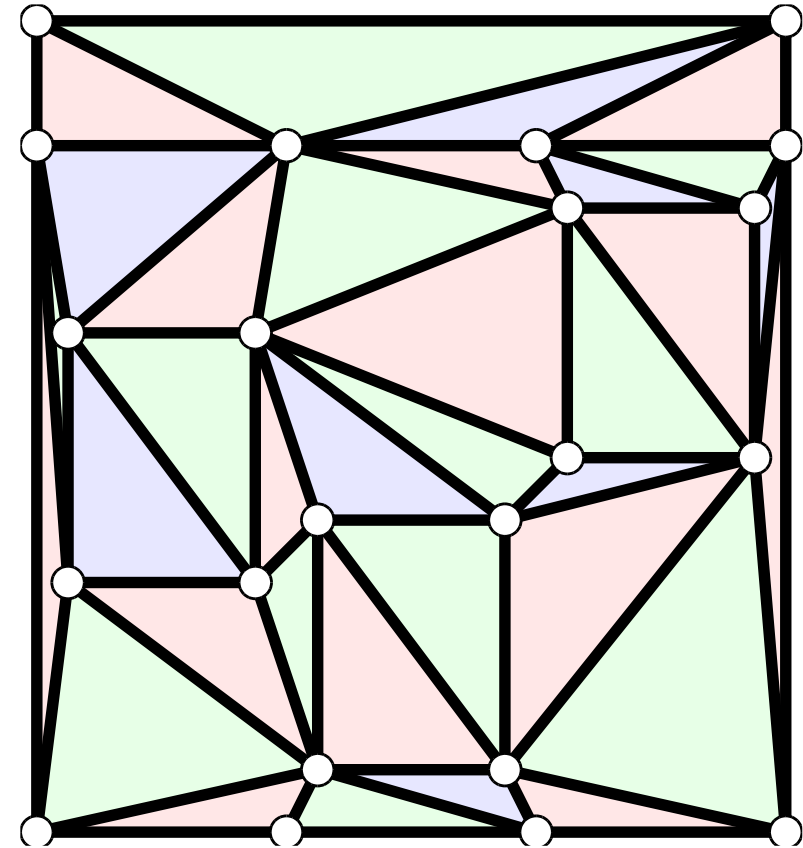
// Delaunay triangulation



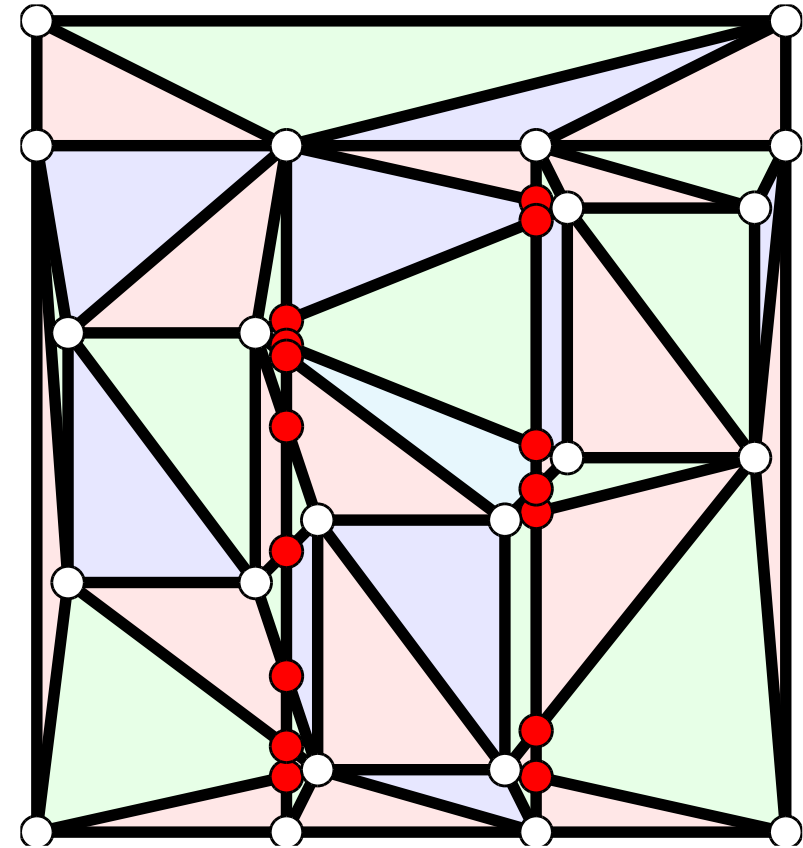
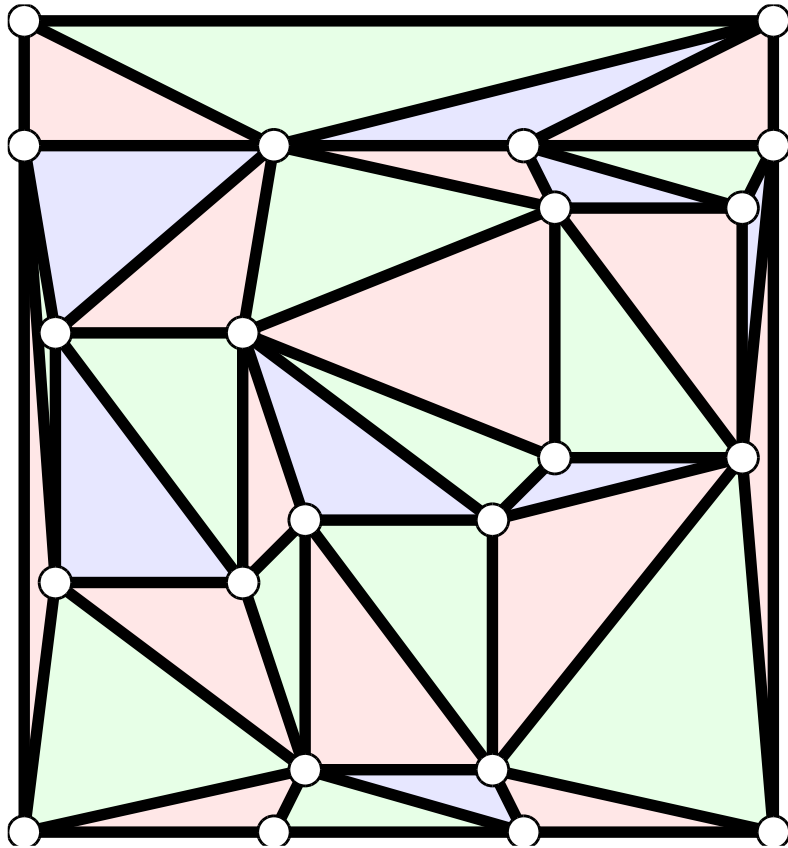
Procedure – step 2 – triangulation

// Delaunay triangulation

// 34 triangles

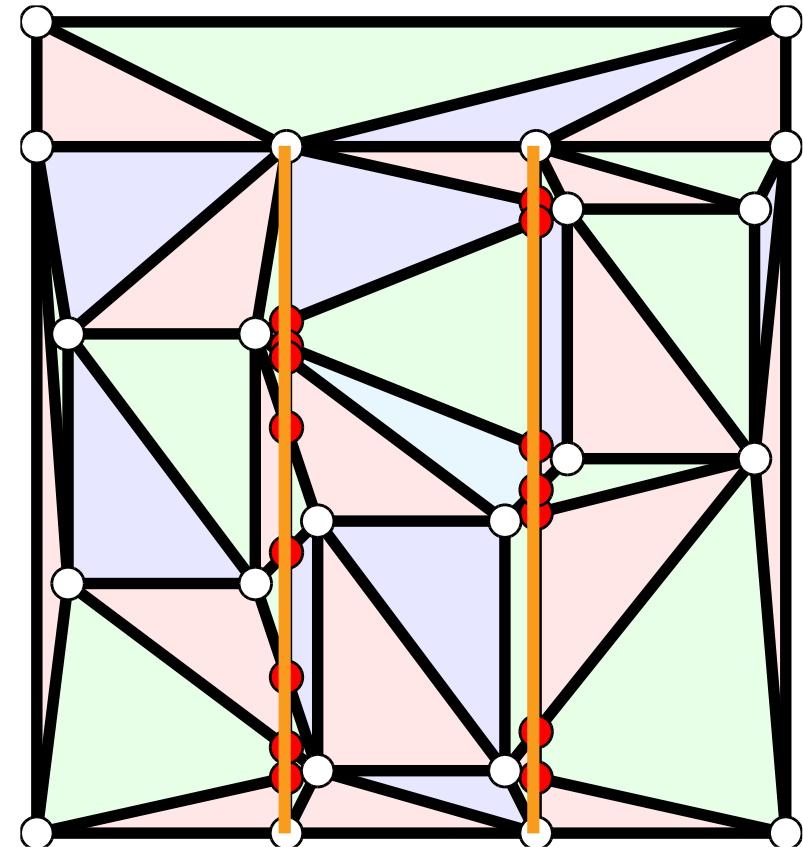


Procedure – step 3 – reconstruction



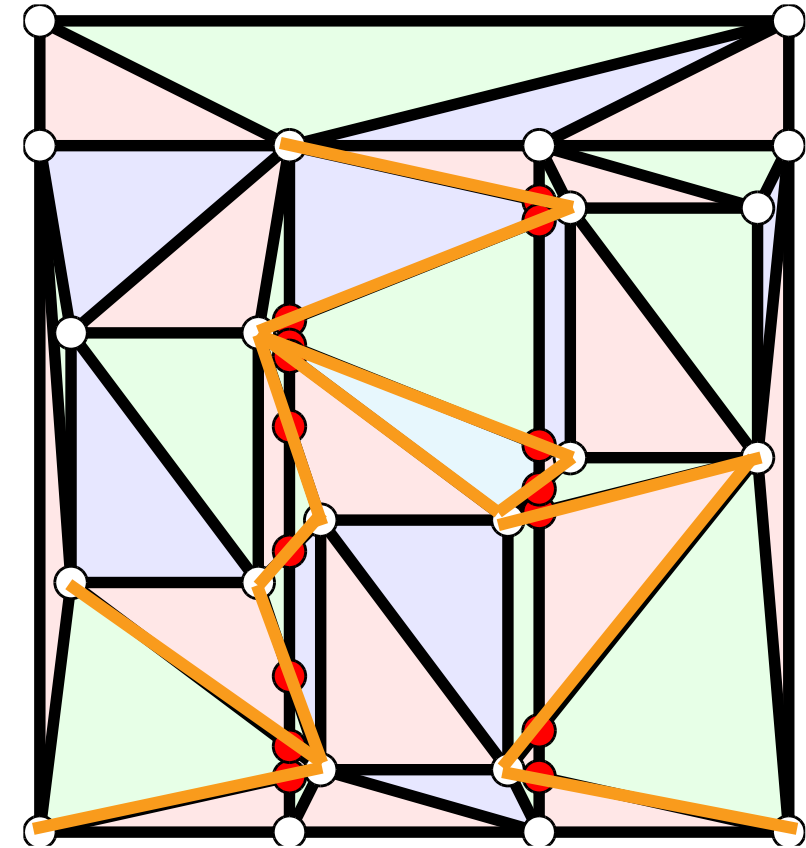
Procedure – step 3 – reconstruction

// Reconstruction of the remaining edges



Procedure – step 3 – reconstruction

- // Reconstruction of the remaining edges
 - // Search for edges to be intersected

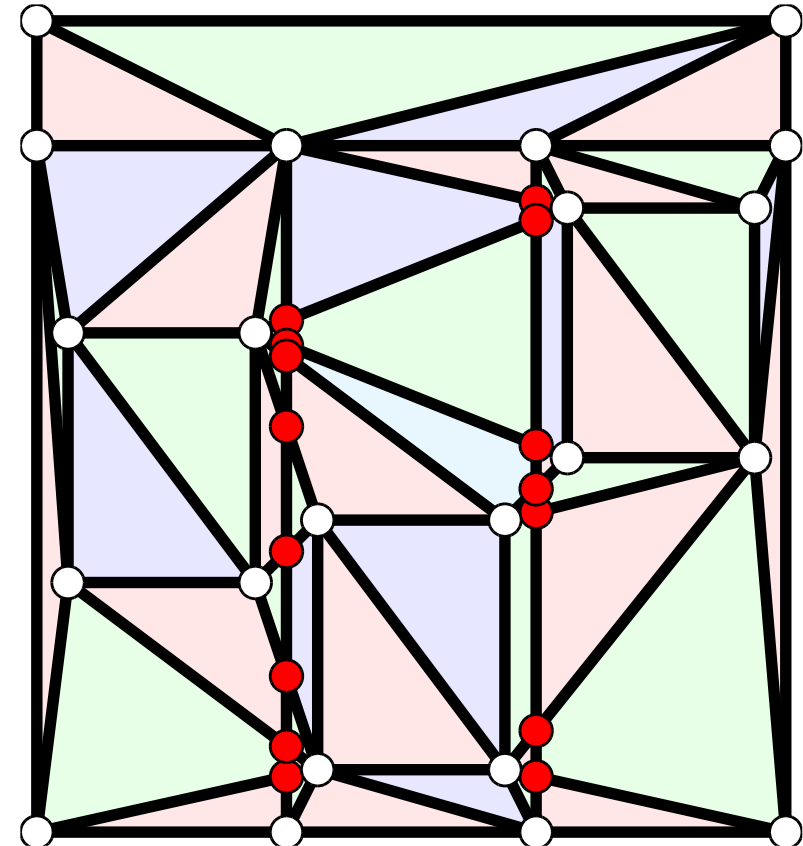


Procedure – step 3 – reconstruction

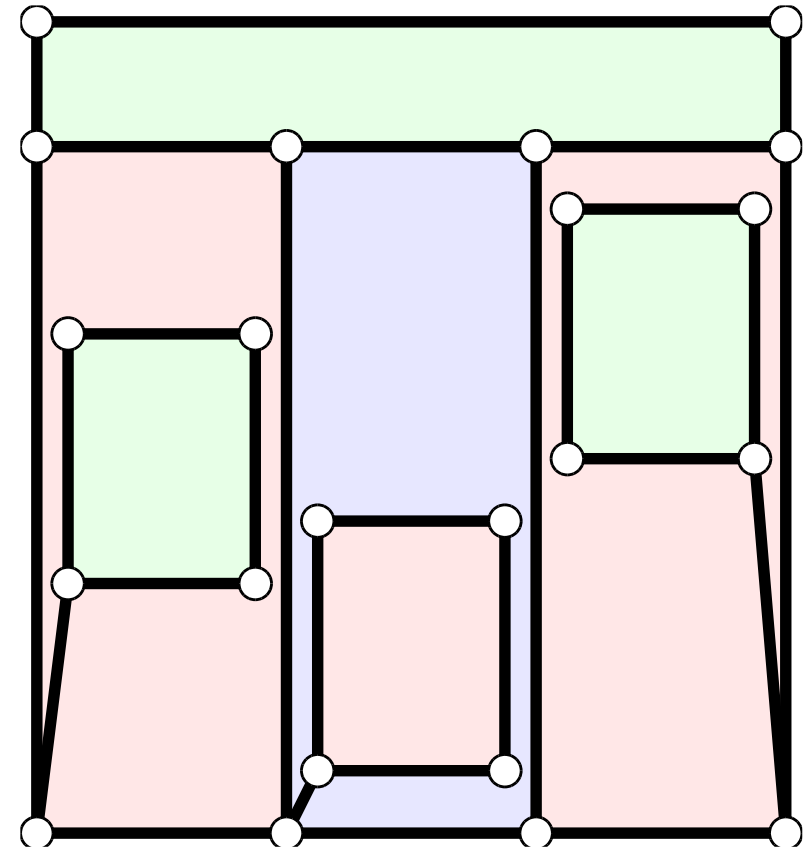
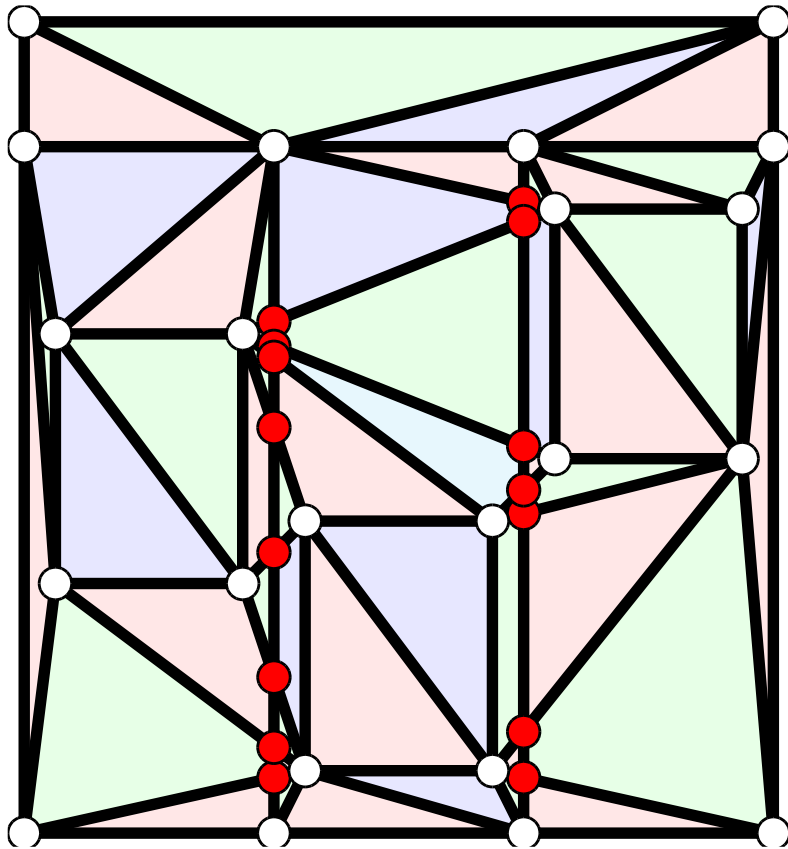
// Reconstruction of the remaining edges

// Search for edges to be intersected

// Calculation of intersection points with the mesh from triangulation

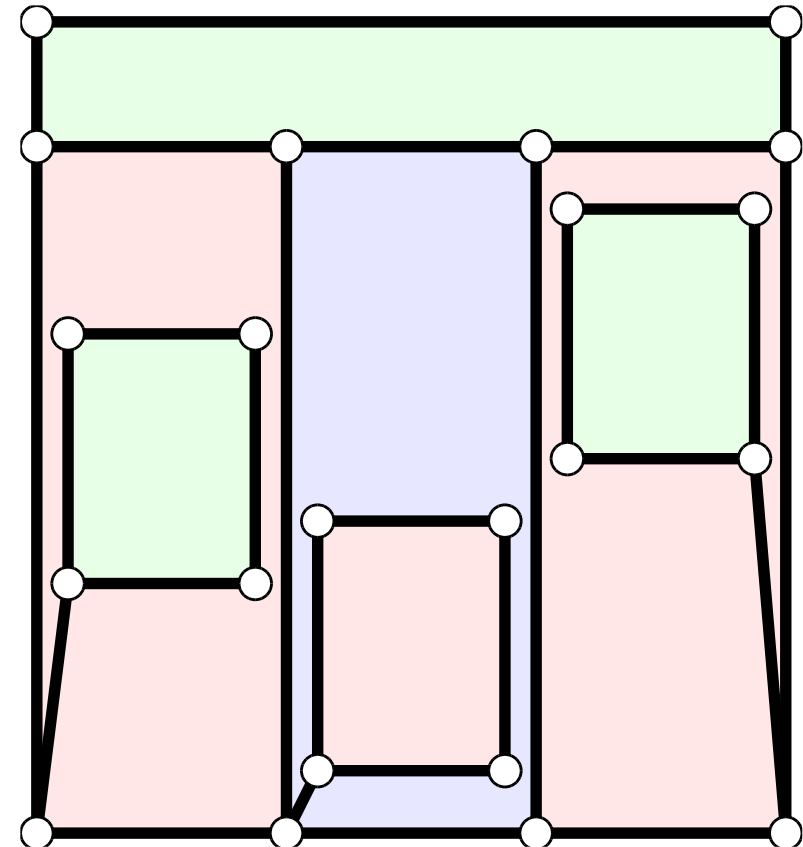


Procedure – step 4 –assignment and clean-up



Procedure – step 4 –assignment and clean-up

- // Assignment of feature-ids to polygons, edges and vertices
- // Removal of unnecessary edges, faces and vertices

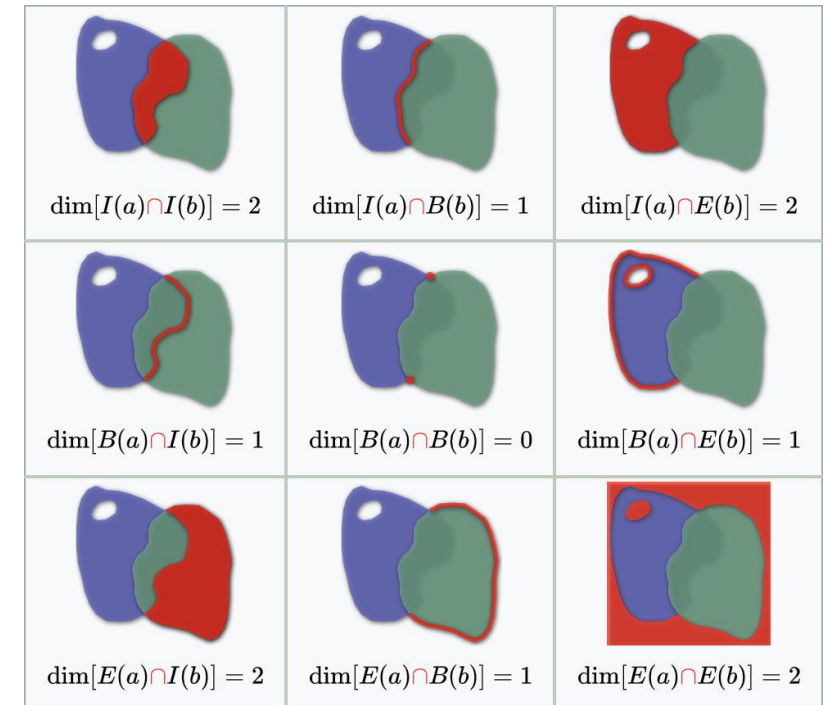


DE-9IM matrices

$$DE9IM(a, b) = \begin{bmatrix} \dim(I(a) \cup I(b)) & \dim(I(a) \cup B(b)) & \dim(I(a) \cup E(b)) \\ \dim(B(a) \cup I(b)) & \dim(B(a) \cup B(b)) & \dim(B(a) \cup E(b)) \\ \dim(E(a) \cup I(b)) & \dim(E(a) \cup B(b)) & \dim(E(a) \cup E(b)) \end{bmatrix}$$

I... Interior
B... Boundary
E... Exterior

// Simple and unambiguous way to represent spatial relationships



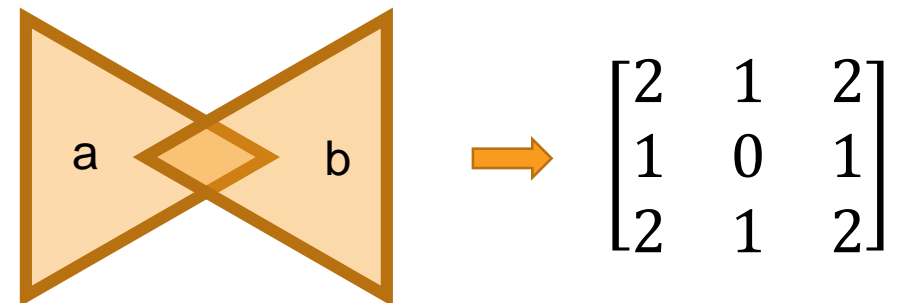
Source: DE-9IM-logoSmall.png (976x862) (wikimedia.org)

DE-9IM matrices

$$DE9IM(a, b) = \begin{bmatrix} \dim(I(a) \cup I(b)) & \dim(I(a) \cup B(b)) & \dim(I(a) \cup E(b)) \\ \dim(B(a) \cup I(b)) & \dim(B(a) \cup B(b)) & \dim(B(a) \cup E(b)) \\ \dim(E(a) \cup I(b)) & \dim(E(a) \cup B(b)) & \dim(E(a) \cup E(b)) \end{bmatrix}$$

I... Interior
B... Boundary
E... Exterior

// Simple and unambiguous way to represent spatial relationships



Source: [DE-9IM-logoSmall.png \(976x862\) \(wikimedia.org\)](#)

Dimension-based feature sets

	0-Dimension Vertex	1-Dimension HalfEdge	2-Dimension Face
Interior	Dim0Set Dim1Set Dim2Set	Dim1Set Dim2Set	Dim2Set
Boundary	Dim1Set ^a Dim2Set	Dim2Set	

Dimension-based feature sets

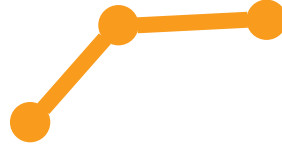
// **Point** features correspond to Dim0Set objects

	0-Dimension Vertex	1-Dimension HalfEdge	2-Dimension Face
Interior	Dim0Set Dim1Set Dim2Set	Dim1Set Dim2Set	Dim2Set
Boundary	Dim1Set ^a Dim2Set	Dim2Set	

Dimension-based feature sets

// **Point** features correspond to Dim0Set objects

// **LineStrings** correspond to Dim1Set objects



	0-Dimension Vertex	1-Dimension HalfEdge	2-Dimension Face
Interior	Dim0Set		
	Dim1Set	Dim1Set	
	Dim2Set	Dim2Set	Dim2Set
Boundary	Dim1Set ^a		
	Dim2Set	Dim2Set	

Dimension-based feature sets

// **Point** features correspond to Dim0Set objects

// **LineStrings** correspond to Dim1Set objects

// **Polygons** correspond to Dim2Set objects



	0-Dimension Vertex	1-Dimension HalfEdge	2-Dimension Face
Interior	Dim0Set Dim1Set	Dim1Set	Dim2Set
Boundary	Dim1Set ^a Dim2Set	Dim2Set	

Test design

1. Do the features meet the requirements for OGC simple features?



Test design

1. Do the features meet the requirements for OGC simple features?
2. Are there overlapping parcels?



Test design

1. Do the features meet the requirements for OGC simple features?
2. Are there overlapping parcels?
3. Are there gaps between parcels?



Test design





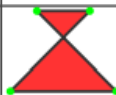



1. Do the features meet the requirements for OGC simple features?
2. Are there overlapping parcels?
3. Are there gaps between parcels?
4. On which parcels is a building located?



Test 1: Requirements for OGC Simple Features









Checking for functionality with simple test files.

Validations always performed at import.

#	Defect	Processing step	WKT or figure
1	consecutive identical points	feature / import	POLYGON ((0 0,2 0,2 0,...))
2	too few points		POLYGON ((0 0))
3	not closed		POLYGON ((0 0,2 0,1 1,0 1))
4	point used twice		
5	overlapping edges		POLYGON ((0 0,0 1,0 0))
6	empty polygon		POLYGON ()
7	wrong orientation		
8	inner polygon is outside		
9	more than one vertex connected to the inner polygon		
10	self intersection	decomposition / generation	
11,12,13	inner face shares outer edge		
14	Test 2 (overlap)	decomposition / query	
15	Test 3 (gap)		

Test 1: Requirements for OGC Simple Features

- // Checking for functionality with simple test files.
- // Validations always performed at import.
- // All defects detected,
 - // with our algorithm
 - // with FME.

#	Defect	Processing step	WKT or figure
1	consecutive identical points	feature / import	POLYGON ((0 0,2 0,2 0,...))
2	too few points		POLYGON ((0 0))
3	not closed		POLYGON ((0 0,2 0,1 1,0 1))
4	point used twice		
5	overlapping edges		POLYGON ((0 0,0 1,0 0))
6	empty polygon		POLYGON ()
7	wrong orientation		
8	inner polygon is outside		
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10	self intersection	decomposition / generation	
11,12,13	inner face shares outer edge		
14	Test 2 (overlap)	decomposition / query	
15	Test 3 (gap)		

Test 2: Are there overlapping parcels?

// 1040 parcels



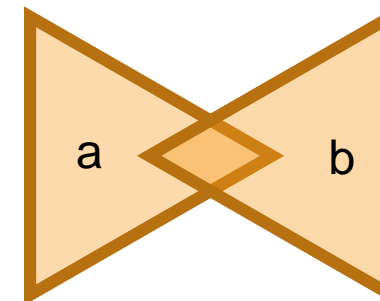
Test 2: Are there overlapping parcels?

// 1040 parcels

// Search with simple set operations.



$$\text{relate}(a, b) = \begin{pmatrix} 2 & * & * \\ * & * & * \\ * & * & * \end{pmatrix}$$

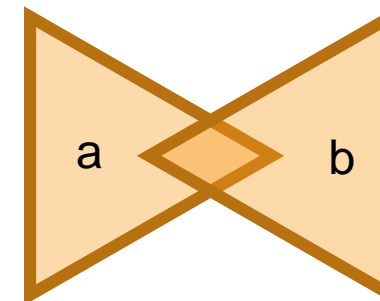


Test 2: Are there overlapping parcels?

- // 1040 parcels
- // Search with simple set operations.
- // No overlapping parcels found,
 - // with our algorithm
 - // with FME.



$$\text{relate}(a, b) = \begin{pmatrix} 2 & * & * \\ * & * & * \\ * & * & * \end{pmatrix}$$

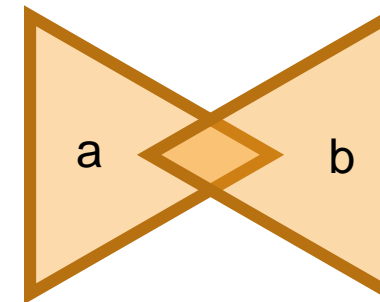
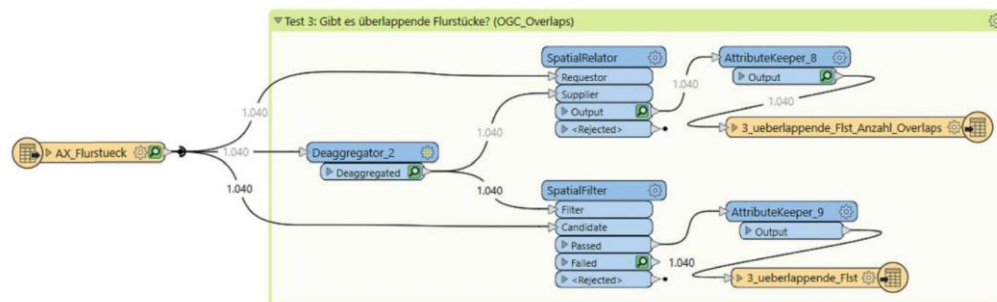


Test 2: Are there overlapping parcels?



- // 1040 parcels
- // Search with simple set operations.
- // No overlapping parcels found,
 - // with our algorithm
 - // with FME.

$$relate(a, b) = \begin{pmatrix} 2 & * & * \\ * & * & * \\ * & * & * \end{pmatrix}$$



Test 3: Are there gaps between parcels?

// 1040 parcels



Test 3: Are there gaps between parcels?

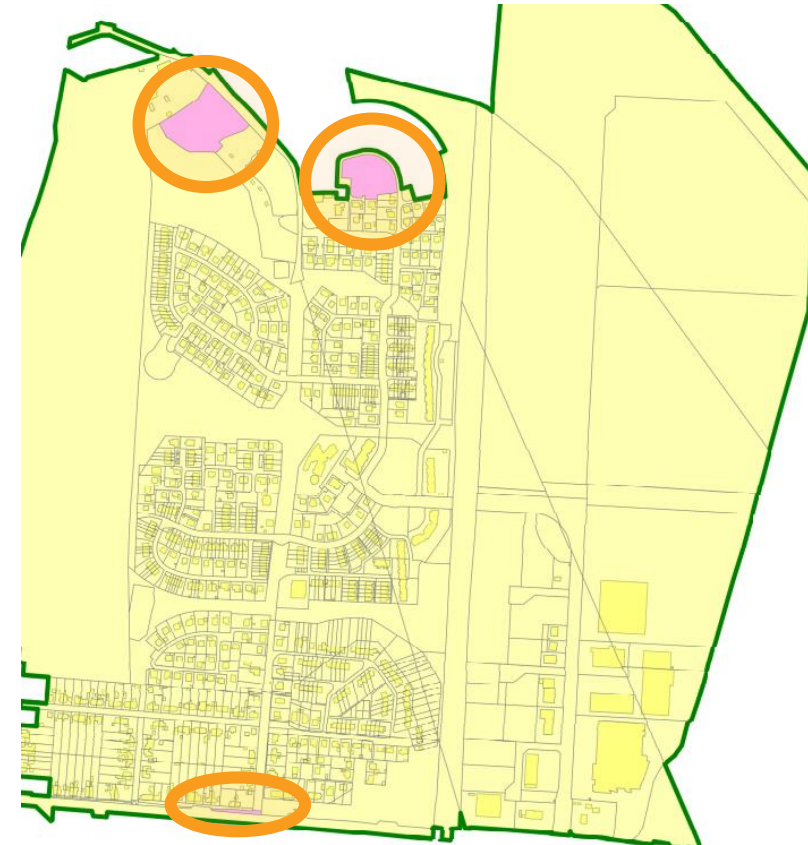


// 1040 parcels

// Simple search for faces without id.

Test 3: Are there gaps between parcels?

- // 1040 parcels
- // Simple search for faces without id.
- // 3 regions found,
- // with our algorithm
- // with FME.

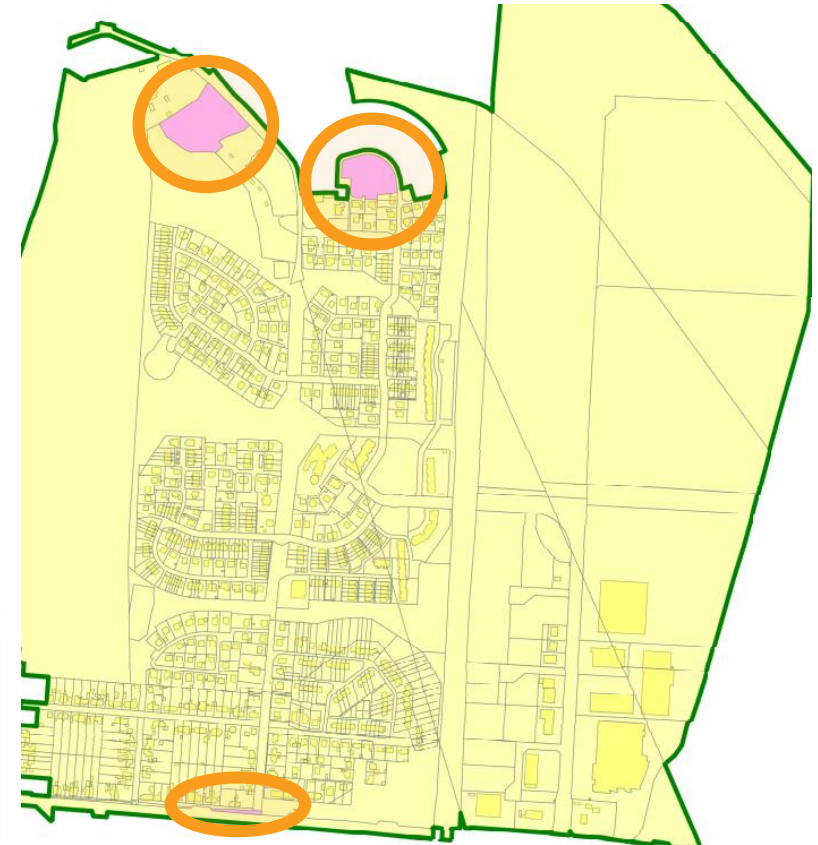
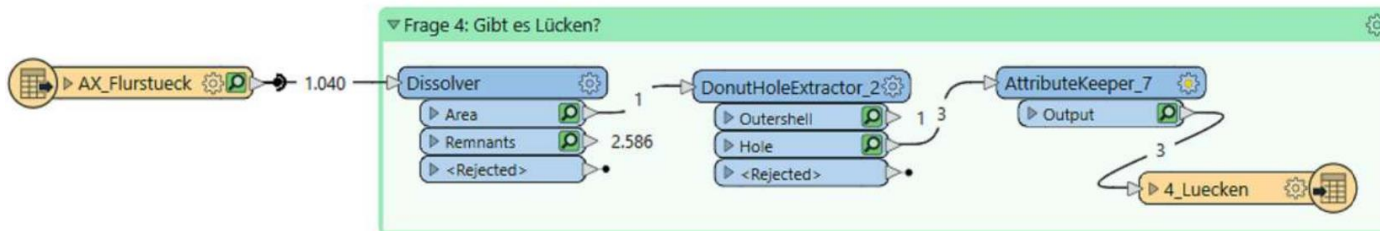


Test 3: Are there gaps between parcels?



- // 1040 parcels
- // Simple search for faces without id.

- // 3 regions found,
- // with our algorithm
- // with FME.



Test 4: On which parcels is a building located?



// 1040 parcels, 1068 Buildings

Test 4: On which parcels is a building located?



- // 1040 parcels, 1068 Buildings
- // Search with simple set operations.
 - // Buildings on parcels

$$\text{relate}(a, b) = \begin{pmatrix} 2 & * & * \\ * & * & * \\ * & * & * \end{pmatrix}$$

Test 4: On which parcels is a building located?



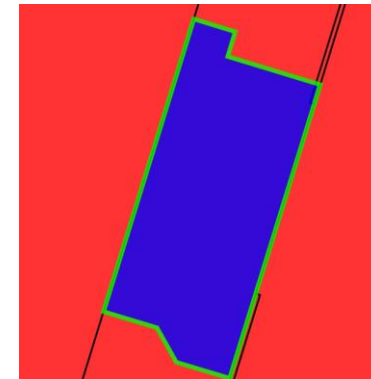
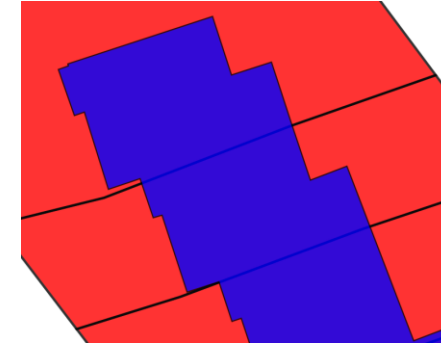
- // 1040 parcels, 1068 Buildings
- // Search with simple set operations.
 - // Buildings on parcels
 - // Buildings on boundaries

$$\text{relate}(a, b) = \begin{pmatrix} 2 & * & * \\ * & * & * \\ * & * & * \end{pmatrix}$$

$$\text{relate}(a, b) = \begin{pmatrix} * & * & * \\ * & 1 & * \\ * & * & * \end{pmatrix}$$

Test 4: On which parcels is a building located?

- // 1040 parcels, 1068 Buildings
- // Search with simple set operations.
 - // Buildings on parcels
 - // Buildings on boundaries
- // Same results
 - // with our algorithm
 - // and with FME.





Conclusion and Outlook

- // Functionality of our approach is proven.
- // Due to set operations always unambiguous results and easily scalable.



Conclusion and Outlook

- // Functionality of our approach is proven.
- // Due to set operations always unambiguous results and easily scalable.
- // Can also be used in other areas such as TLS or clash detection.
- // Use in the three-dimensional field is under development.

Conclusion and Outlook

- // Functionality of our approach is proven.
- // Due to set operations always unambiguous results and easily scalable.
- // Can also be used in other areas such as TLS or clash detection.
- // Use in the three-dimensional field is under development.

Kraft B (2016) Ein verfahren der raumzerlegung als grundlage zur prüfung von geometrie und topologie digitaler bauwerksmodelle. DOI 10.14279/depositonce-5117

Huhnt W (2018) Reconstruction of edges in digital building models. *Advanced Engineering Informatics* 38:474–487, DOI <https://doi.org/10.1016/j.aei.2018.08.004>

Vetter J (2019) Eine untersuchung zum aufwand bei der berechnung einer raumzerlegung im 2d aus einer gegebenen menge an polygone. Master's thesis, Technische Universität, Berlin

Vetter J, Huhnt W (2021) Accuracy aspects when transforming a boundary representation of solids into a tetrahedral space partition. In: *Proceedings of the EG-ICE 2021 Workshop on Intelligent Computing in Engineering*, Universitätsverlag TU Berlin, Germany, pp 320–329

Romanschek E, Clemen C, Huhnt W (2020) From terrestrial laser scans to a surface model of a building: Proof of concept in 2d. In: Ungureanu L, Hartmann T (eds) *EG-ICE 2020 Proceedings*, Universitätsverlag TU Berlin, pp 432–442

Romanschek E, Clemen C, Huhnt W (2021) A novel robust approach for computing de-9im matrices based on space partition and integer coordinates. *ISPRS International Journal of Geo-Information* 10(11), DOI 10.3390/ijgi10110715